

# Intelligent Control Systems: Qualitative modelling – Tutorial

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# Normalized intervals

**Qualitative range space:** for variables with "normal"  $N$  value

$$\mathcal{Q} = \{H, N, L, 0\}, \quad \mathcal{B} = \{0, 1\}, \quad \mathcal{Q}_E = \{H, N, L, 0, e+, e-\}$$

Operation table for addition

$[a] + [b]$	0	$L$	$N$	$H$
0	0	$L$	$N$	$H$
$L$	$L$	$N$	$H$	$e+$
$N$	$N$	$H$	$e+$	$e+$
$H$	$H$	$e+$	$e+$	$e+$

**TASK:** Construct (a possible) operation table for multiplication

## (A possible) Solution

$[a] * [b]$	0	$L$	$N$	$H$
0	0	0	0	0
$L$	0	$L$	$L$	$N$
$N$	0	$L$	$N$	$H$
$H$	0	$N$	$H$	$H$

TASK: Construct another possible operation table for the multiplication.

# Confluences

Given a tank with in- and outflow, and a possible hole at the bottom of the tank.

The dynamic model originates from the mass balance

$$\frac{dm}{dt} = v_{in} - v_{out} - \kappa m$$

where  $\kappa \in \{0, 1\}$  is the fault (hole) indicator variable.

**TASK:** Derive the confluence from the model, and give its solution. Derive the set of rules from the confluence.

# Qualitative difference equation models

Given a (static) model of a sensor that suffers from a multiplicative bias over the normalized qualitative range set  $\mathcal{Q}$ :

$$[x^m](k) = [x](k) * \chi_{M_x}$$

where  $[x] \in \mathcal{Q}$  is the real value,  $[x^m] \in \mathcal{Q}_E$  is the value indicated by the (possibly faulty) sensor), and  $\chi_{M_x} \in \{L, N\}$  is the fault (bias) indicator variable.

Use the qualitative multiplication constructed at the beginning of the tutorial.

**TASK:** Give the solution table of the qualitative model.

Construct rules from the rows of the solution table.